

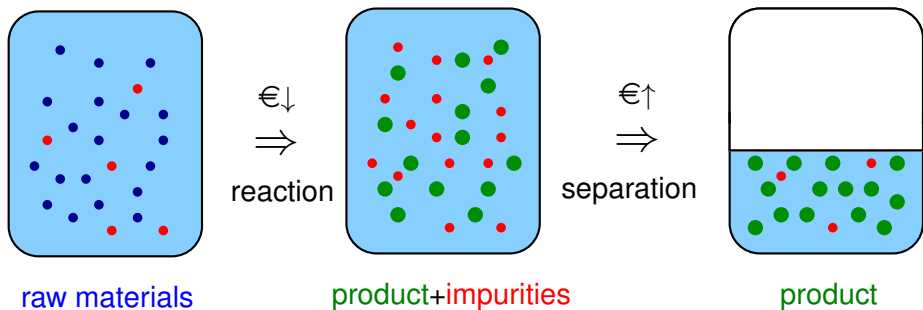
EXPERIMENTAL VALIDATION AND COMPARISON OF
TIME-OPTIMAL AND INDUSTRIAL STRATEGY FOR
MEMBRANE SEPARATION PROCESS

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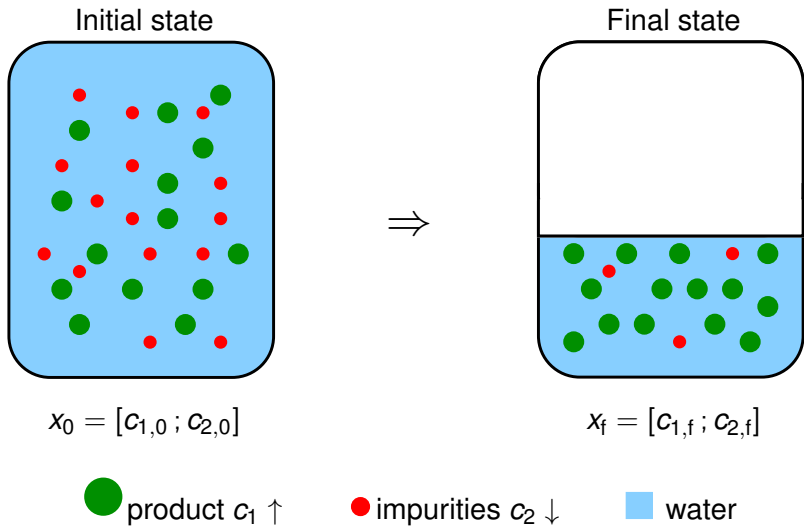
Faculty of Chemical and Food Technology
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Profit €

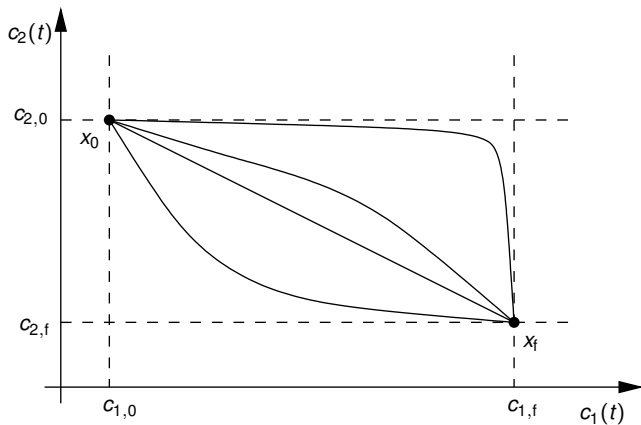
- production in (bio)chemical industry → profit



- control must - guarantee the product quality (purity)
- optimize the profit (production cost)

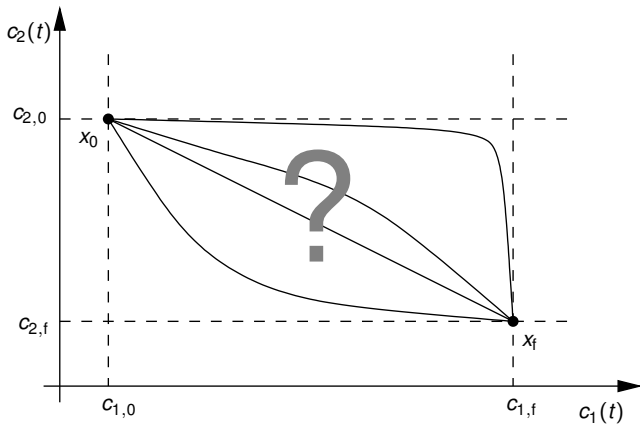


BATCH PROCESS GOAL

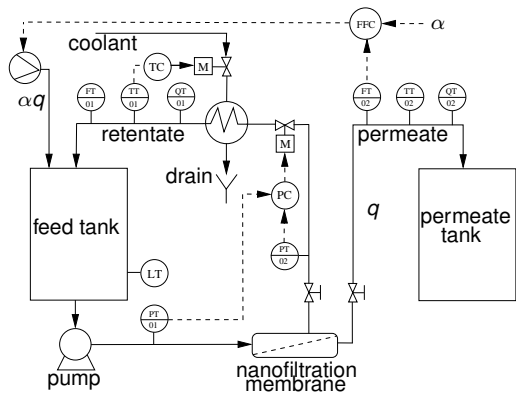


$x_0 \rightarrow x_f \Leftrightarrow \begin{cases} \bullet \text{ product } c_1 \uparrow \\ \bullet \text{ impurities } c_2 \downarrow \end{cases}$

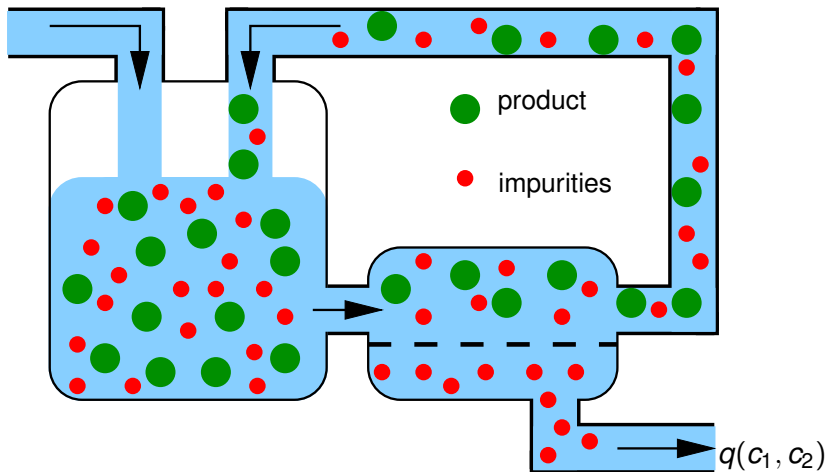
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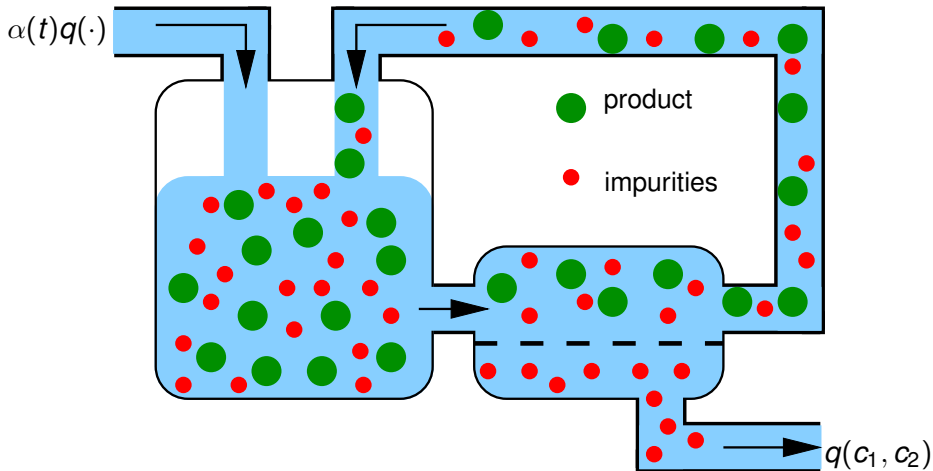


- transmembrane pressure: controlled at fixed value (wear-and-tear)
- temperature: controlled at fixed value (product degradation)



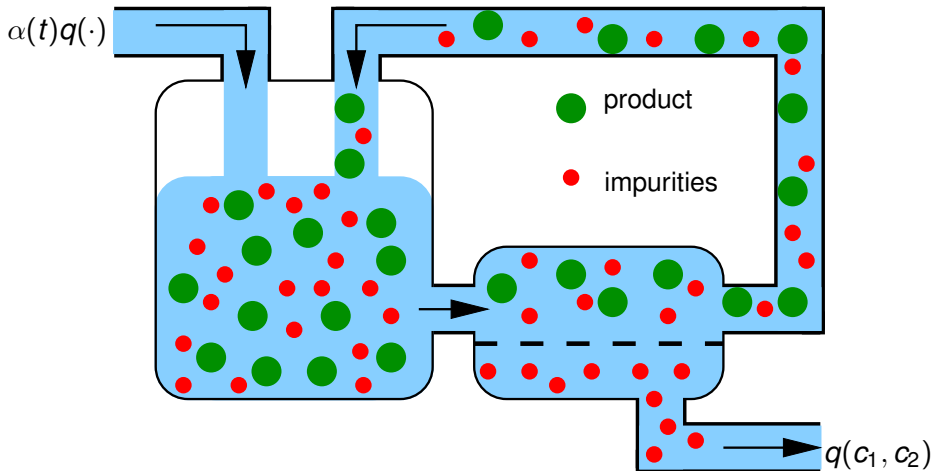
– membrane model: permeate flow $q(c_1, c_2)$

PROCESS DESCRIPTION

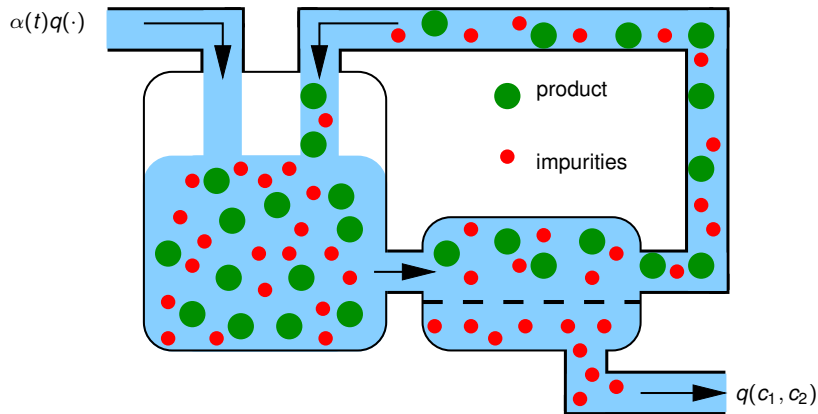


– concentrations dynamically adjusted by the water inflow $\alpha(t)q(\cdot)$

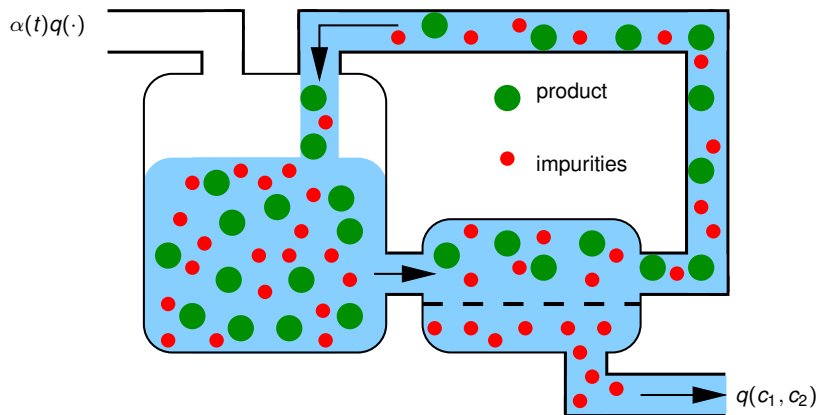
OPTIMIZATION GOAL



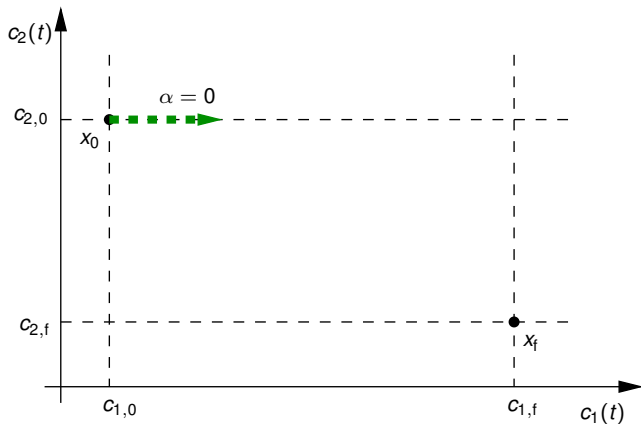
– find $\alpha(t)$ to minimize final (batch) time



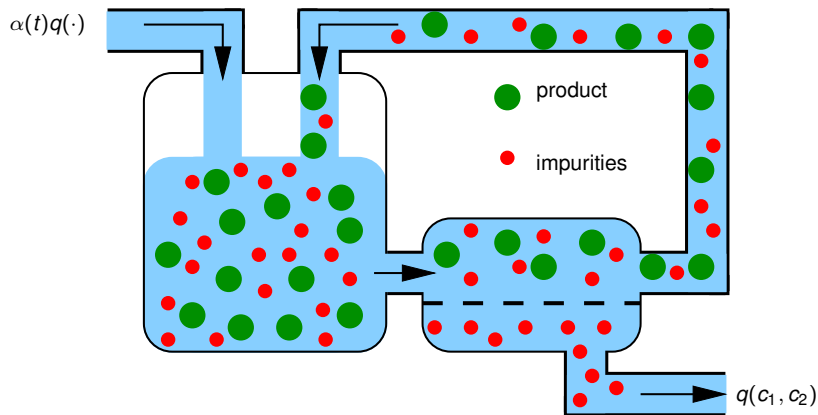
– manipulated variable: $\alpha(t) \in [0, \infty)$



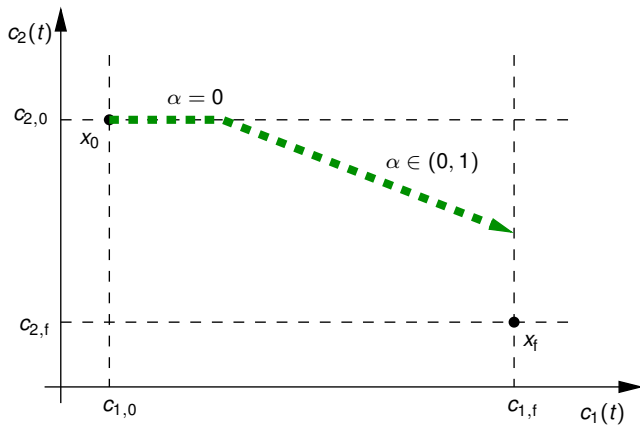
– concentration mode: $\alpha(t) = 0$ $c_1 \uparrow$ $c_2 \approx \text{const.}$



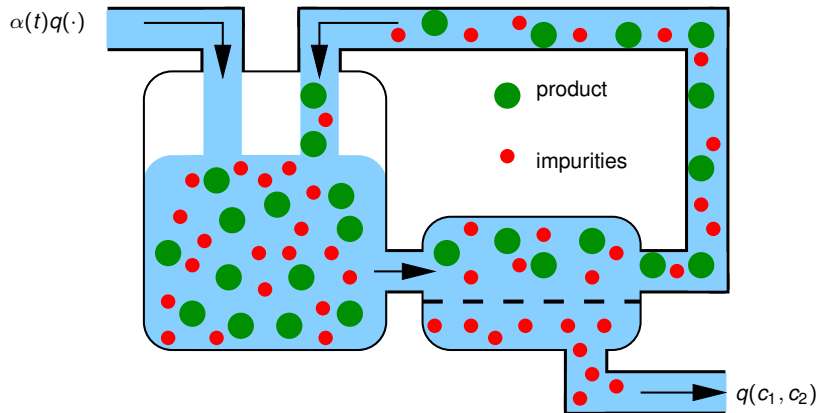
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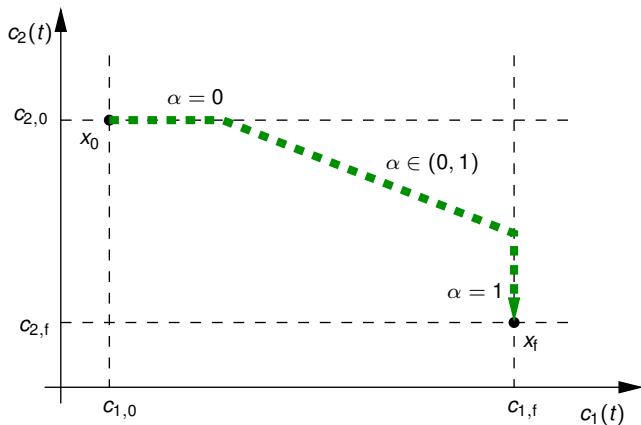
– variable volume diafiltration: $\alpha(t) \in (0, 1)$ $c_1 \uparrow$ $c_2 \downarrow$



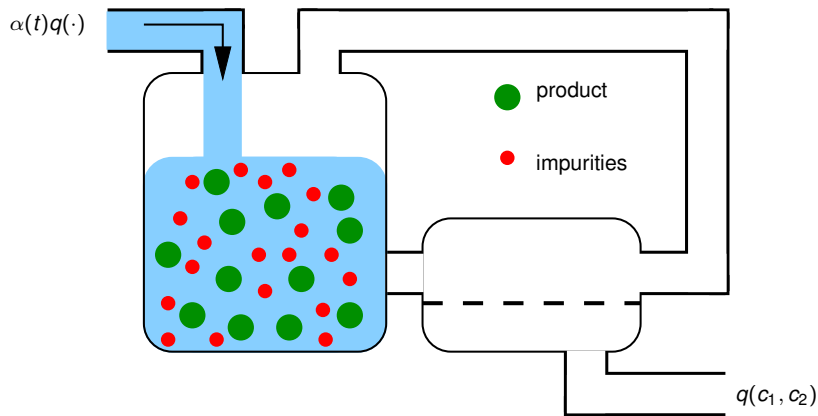
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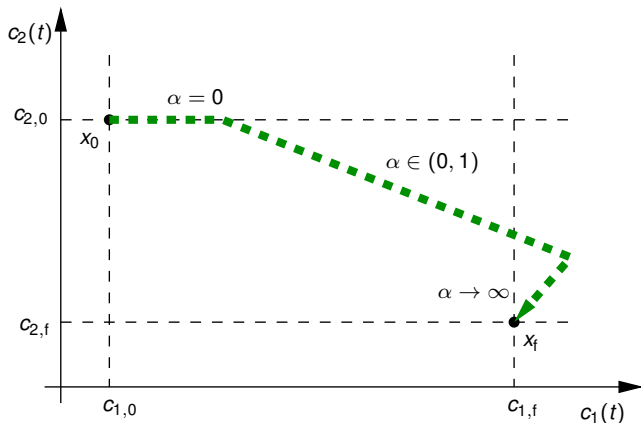
– constant volume diafiltration: $\alpha(t) = 1$ $c_1 \approx \text{const.}$ $c_2 \downarrow$



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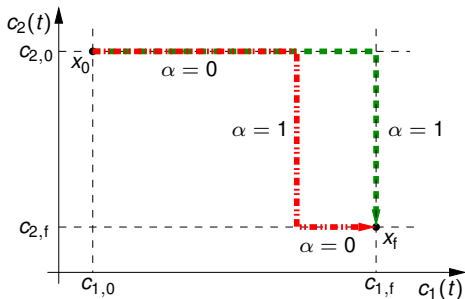
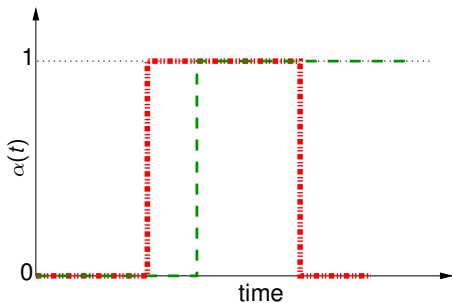
– dilution mode: $\alpha(t) \rightarrow \infty$ $c_1 \downarrow$ $c_2 \downarrow$ $\frac{c_1(t)}{c_2(t)} = \text{const.}$



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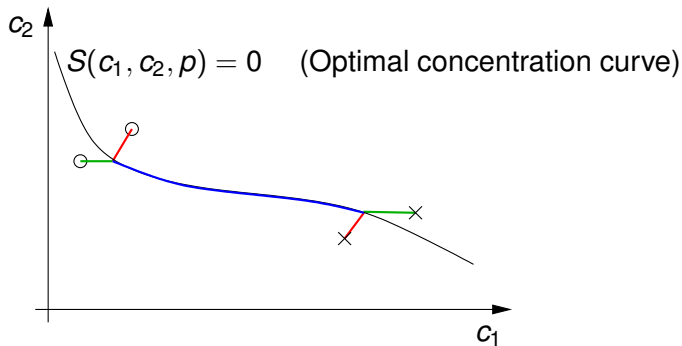
Traditional industrial diafiltration

$$\alpha(t) = \{0, 1\} \text{ or } \{0, 1, 0\}$$



OPTIMAL OPERATION

$$\alpha(t) = \begin{cases} 0 & \text{(if } S(c_{1,0}, c_{2,0}, p) < 0, S(c_{1,f}, c_{2,f}, p) > 0) \\ f(c_1, c_2, p) & \text{if } S(c_1, c_2, p) = 0 \\ \infty & \text{(if } S(c_{1,0}, c_{2,0}, p) > 0, S(c_{1,f}, c_{2,f}, p) < 0) \end{cases}$$



Paulen and Fikar, Optimal Operation of Batch Membrane Processes, *Springer*, 2016.

Two candidate models:

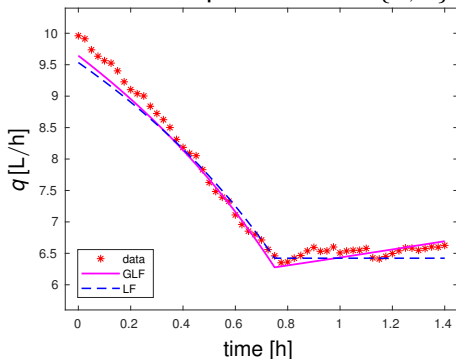
- Generalized limiting flux model (GLF)

$$q = p_1 \ln \left(\frac{p_2}{c_1 c_2^{p_3}} \right)$$

- Limiting flux model (LF)

$$q = p_1 \ln \left(\frac{p_2}{c_1} \right)$$

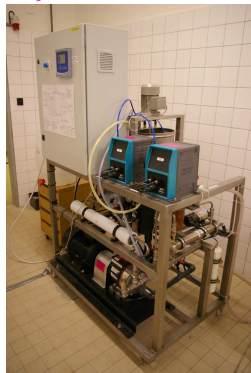
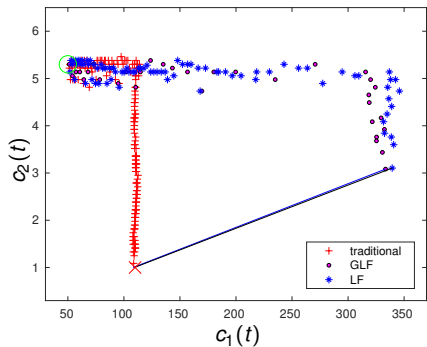
Data fit with operation $\alpha = \{0, 1\}$



Fitting of parameters to the experimental data done using least-squares estimation with dynamic data reconciliation.

EXPERIMENTAL OPTIMAL OPERATION

- Traditional approach: $\alpha = \{0, 1\}$ $t_f = 4.28$ h
- Time minimization (LF model): $\alpha = \{0, 1, \infty\}$ $t_f = 3.85$ h
- Time minimization (GLF model): $\alpha = \{0, 0.91, \infty\}$ $t_f = 3.74$ h



- Optimal operation of diafiltration using analytical approach
- Traditional approaches are mostly suboptimal
- Successfully validated in laboratory conditions
- Seamless realization of the optimal strategy at the existing hardware
- Extensions to explicit consideration of economic (multi-objective) operation
- Extensions to explicit consideration of membrane fouling
- Robust approaches currently studied